

EE1L1 IP-1 Loudspeaker Project 2025-2026

“The Booming Bass”

Overview:

What is sound?

Composition of a loudspeaker

- model of a cone loudspeaker-driver
- a bit of physics
- 1, 2, ... multi driver loudspeaker system
- impedance model
- transfer function

Measurement set-up

- measuring the loudspeaker impedance

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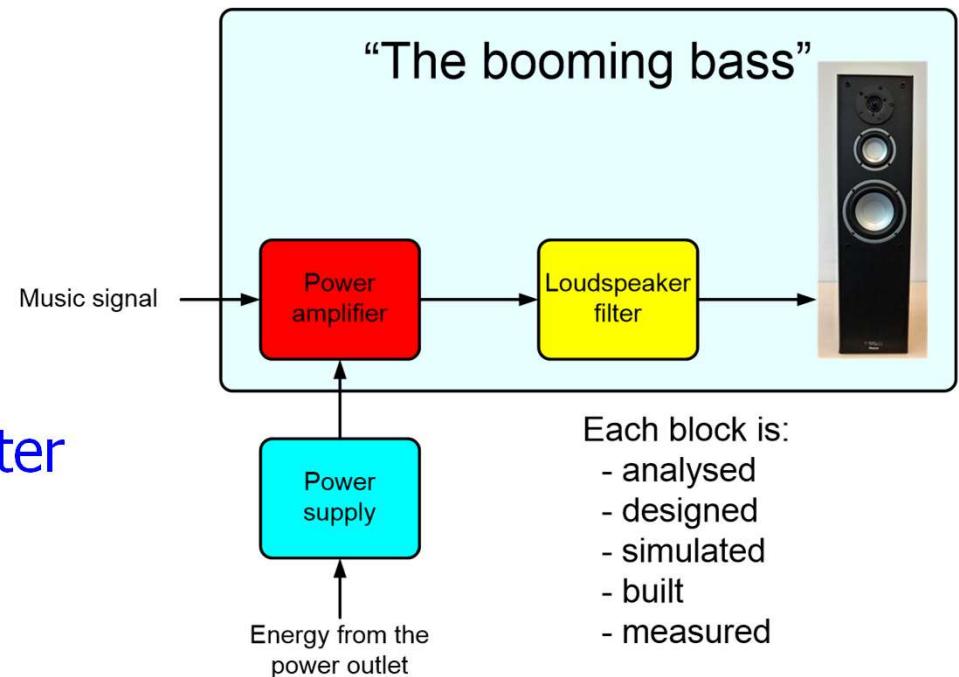
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IP-1 Project: “The booming bass”

Analyzing, designing, simulating, building and testing of an audio system:

- Symmetric power supply
- Audio power amplifier
- Measuring of loudspeakers
- Passive 3-way loudspeaker filter
- “The booming bass”
Linkwitz Transform



What is sound?

Sound is:

- *a wave phenomenon,*
- *a pressure variation which propagates through the medium air with the speed of sound.*

What is the speed of sound and what does it depend on?

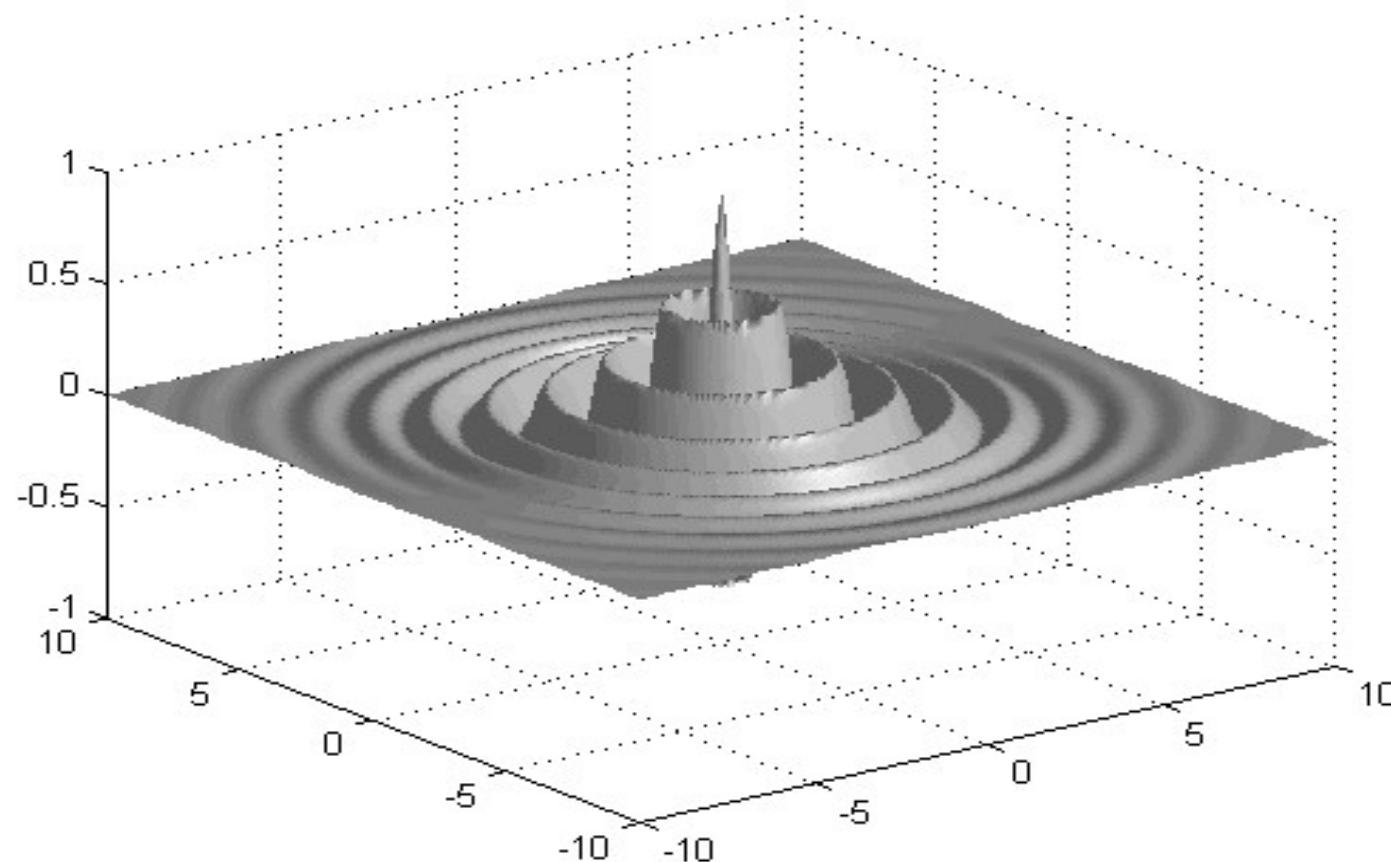
The speed of sound is $v \approx 345$ m/s and depends on temperature, humidity and air pressure.

What determines the pitch?

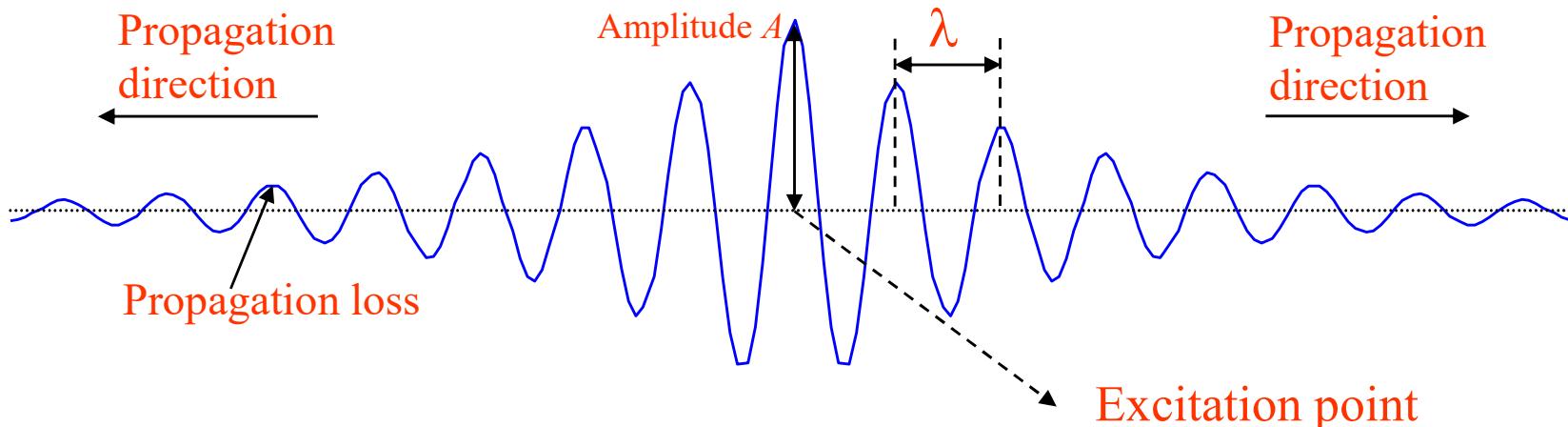
The **pitch or frequency** is determined by the number of (sine shaped) pressure variations per second (unit hertz [Hz]).

Wave propagation

Analogy of wave propagation on the water surface:



Characteristics of a sine sound wave



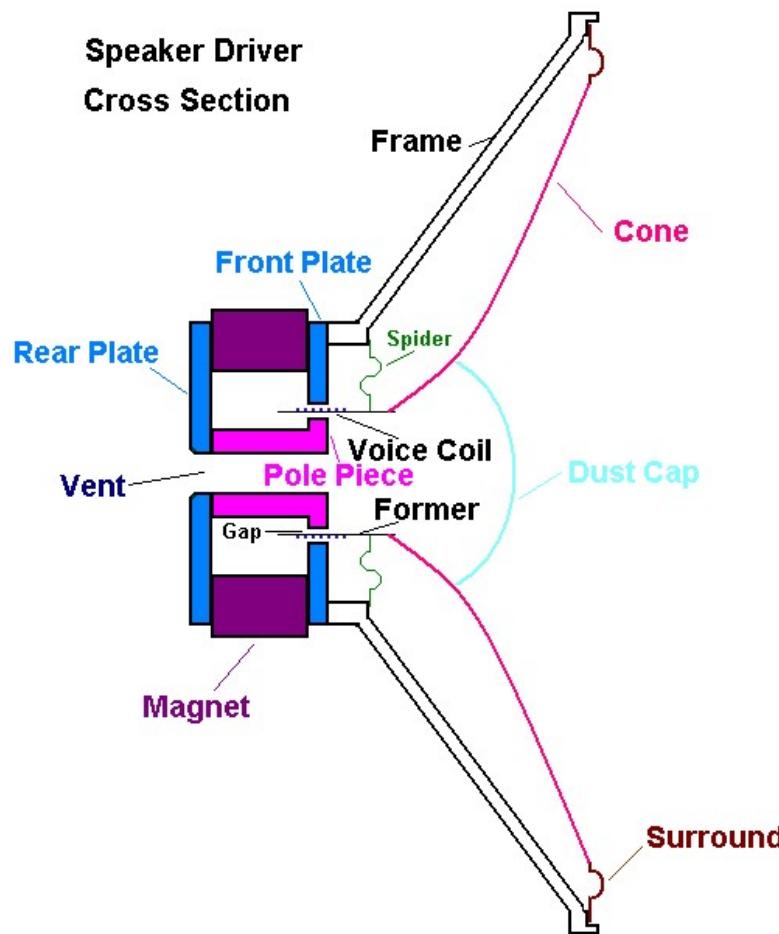
The **wavelength λ** is the distance traveled by the sound during one period of a sine shaped pressure variation.

Fundamental relation between frequency f [Hz], wavelength λ [m] and propagation speed v [m/s]:

$$v = f \cdot \lambda$$

Loudspeaker-driver: electrical side

A loudspeaker-driver is an **electro-mechanical transducer**:
electrical energy is converted into mechanical (acoustical) energy.



Operation of a cone loudspeaker-driver:

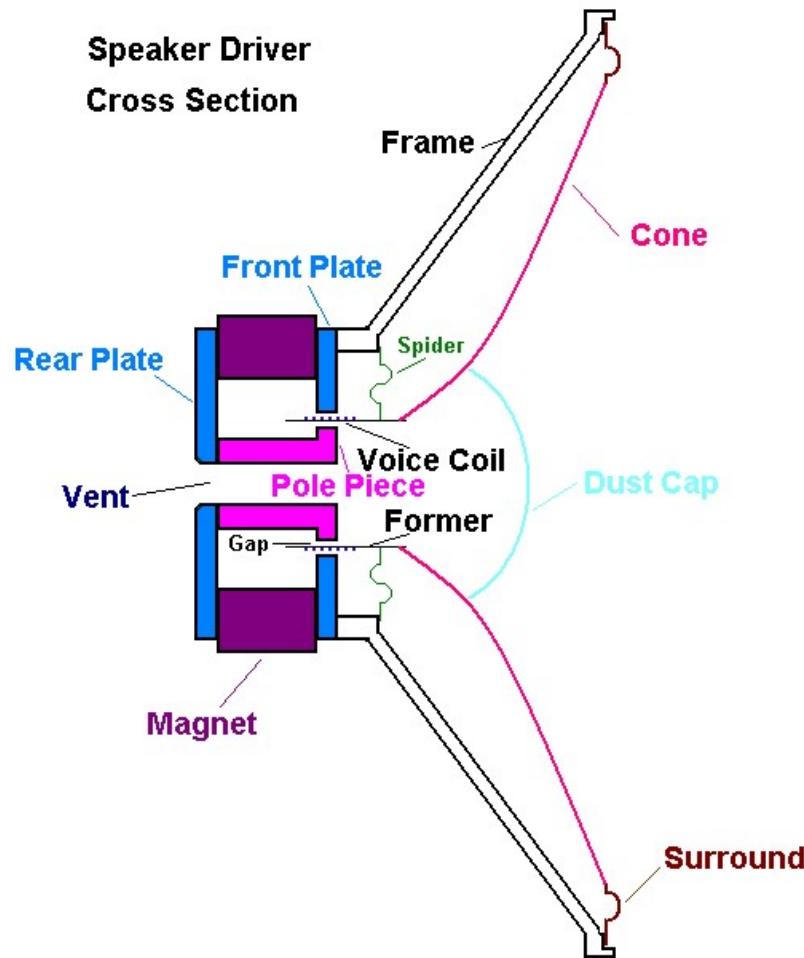
The current \vec{I}_{ls} through the voice coil, perpendicular to the permanent magnetic field \vec{B} in the gap, causes a force on the voice coil:

$$\vec{F}_L = l \cdot \vec{I}_{ls} \times \vec{B}$$

The Lorentz force.

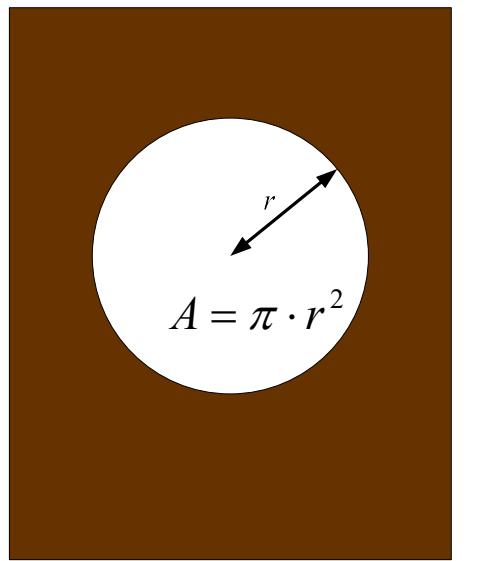
We have a linear motor!

Loudspeaker-driver: mechanical side



- cone movement \Rightarrow pressure variation \Rightarrow sound
- forward cone movement \Rightarrow
 - * increase of pressure at the front
 - * decrease of pressure at the back \Rightarrow loudspeaker "should be" put in a box, otherwise acoustic short-circuit
- the cone is spring-load suspended to the spider and the surround at the outer edge:
 \Rightarrow a mass-spring system with an eigen- or resonance frequency

A bit of acoustic theory (1)



Sound pressure of a moving piston

The sound pressure at a distance d is: $p = \frac{\rho \cdot U \cdot f}{2 \cdot d}$

- p is sound pressure [N/m^2]
- ρ is air density: 1.19 kg/m^3
- $U = A \cdot v$ is volume flow rate [m^3/s]
- f is frequency [Hz]
- d is distance [m]

speed piston: $v(t) = \frac{dx(t)}{dt} = 2\pi f \cdot \hat{x} \cdot \cos 2\pi f t$

acceleration: $a(t) = \frac{dv(t)}{dt} = \frac{d^2x(t)}{dt^2} = -(2\pi f)^2 \cdot \hat{x} \cdot \sin 2\pi f t$

Now it follows with $v_{rms} = \frac{\hat{v}}{\sqrt{2}} = 2\pi f \cdot x_{rms} = \frac{a_{rms}}{2\pi f}$ $x_{rms} = \sqrt{\hat{x}^2} = \frac{\hat{x}}{\sqrt{2}}$ = effective value

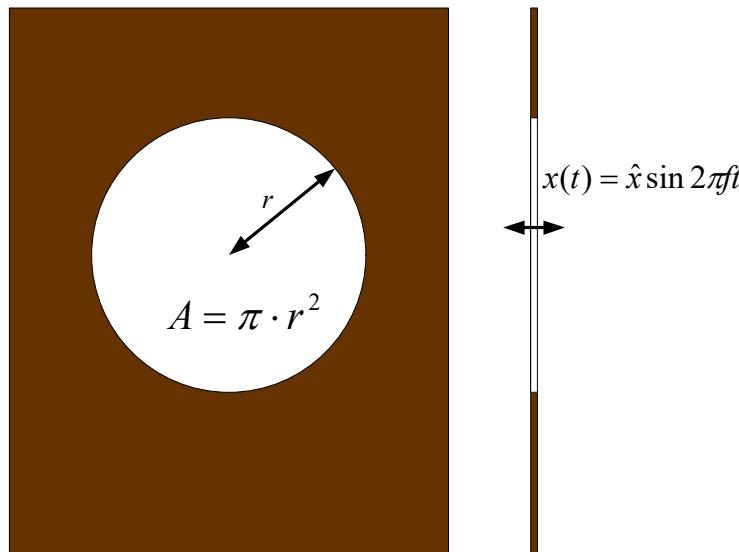
and $p_{rms} = \frac{\rho \cdot U_{rms} \cdot f}{2 \cdot d} = \frac{\rho \cdot A \cdot v_{rms} \cdot f}{2 \cdot d}$

$$= \frac{\rho \cdot A \cdot x_{rms} \cdot \pi \cdot f^2}{d} = \frac{\rho \cdot A \cdot a_{rms}}{4\pi \cdot d}$$

$$\Rightarrow p_{rms} \approx a_{rms} = 2\pi f \cdot v_{rms} = (2\pi f)^2 \cdot x_{rms}$$

A bit of acoustic theory (2)

Current v.s. acceleration v.s. sound pressure:



Sound pressure of a moving piston

$$F_l = B \cdot I_{ls} \cdot l = m \cdot a \quad \text{dus} \quad a \approx I_{ls} \approx V_{ls}$$

- m = mass of the piston + voice coil [kg]
- B = magnetic flux density [T]
- I_{ls} = current through the voice coil [A]
- l = length of the voice coil wire [m]

Thus, the sound pressure, which is proportional to the acceleration a of the piston, is proportional to the voltage at the loudspeaker terminals. Since for constant sound pressure $p_{rms} \approx a_{rms}$, the volume flow rate will decrease with frequency as:

The sound intensity is $I_{ac} \approx p_{rms}^2$ [W/m²]

Sound Pressure Level is:

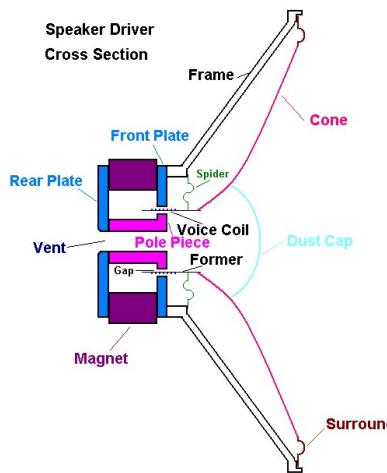
$$SPL = 10 \cdot \log_{10} \frac{p_{rms}^2}{p_{ref}^2} = 20 \cdot \log_{10} \frac{p_{rms}}{p_{ref}} \text{ [dB]}$$

where $p_{ref} = 2 \cdot 10^{-5}$ N/m²

$$v_{rms} = \frac{a_{rms}}{2\pi f} \quad \text{and} \quad x_{rms} = \frac{a_{rms}}{(2\pi f)^2}$$

So, for a constant sound pressure at a 2x lower frequency, a 2x larger volume flow rate and a 4x larger cone displacement is required (for a fixed piston area A).

Acoustic behavior loudspeaker



- to get the same sound level, lower frequencies require a **larger volume flow rate (air displacement / s)** than higher frequencies: lower frequencies => larger driver.
- a larger (and heavier) cone has several disadvantages when used at higher frequencies:
 - * it becomes directive
 - * internal damping of high frequencies
 - * resonances of stiff cone materials (cone break up)

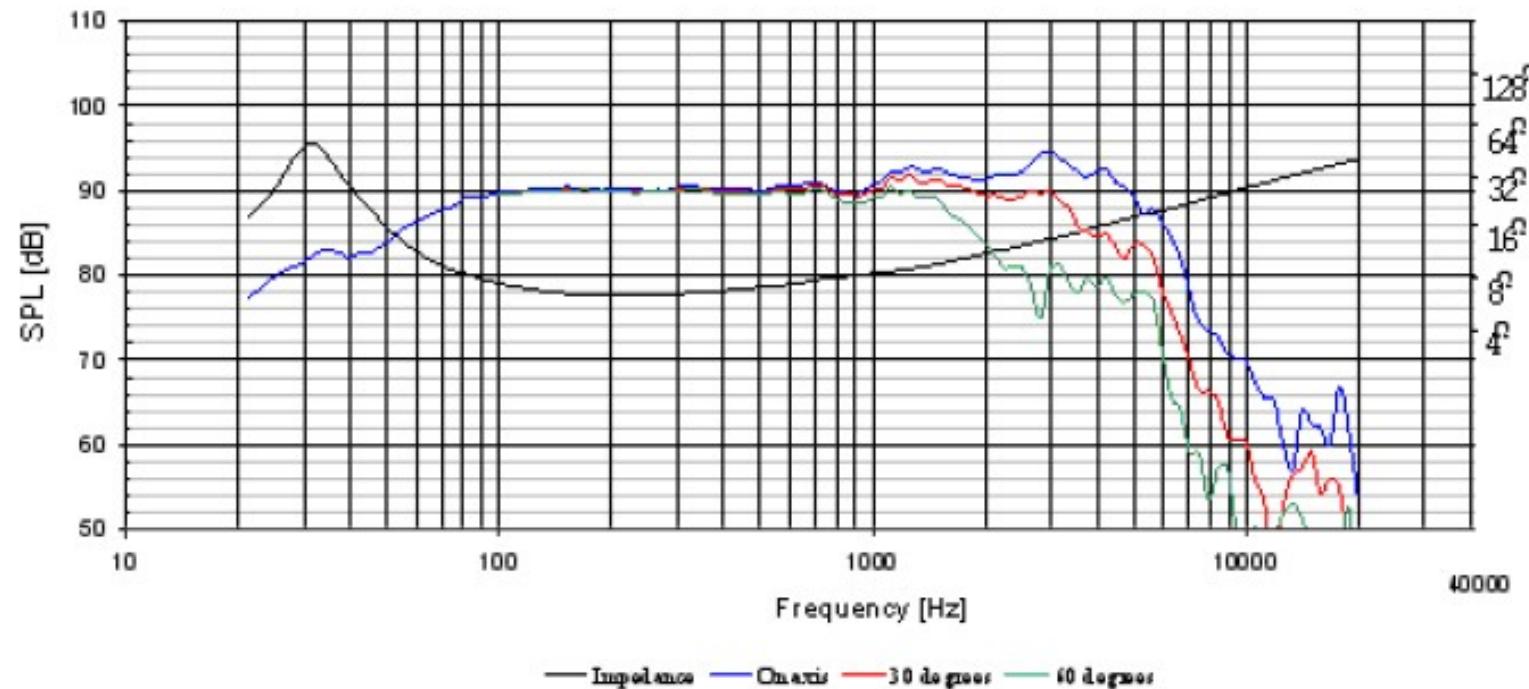
Loudspeaker-drivers are usually designed to reproduce a limited range of frequencies: $10 < f_{\max} / f_{\min} < 100$.

In a loudspeaker system, the frequency range 20 Hz – 20 kHz is therefore often reproduced by 2 or 3 loudspeaker-drivers, that each cover a part of the frequency range:

- * bass and treble: **2-way system**
- * bass, mid and treble: **3-way system**

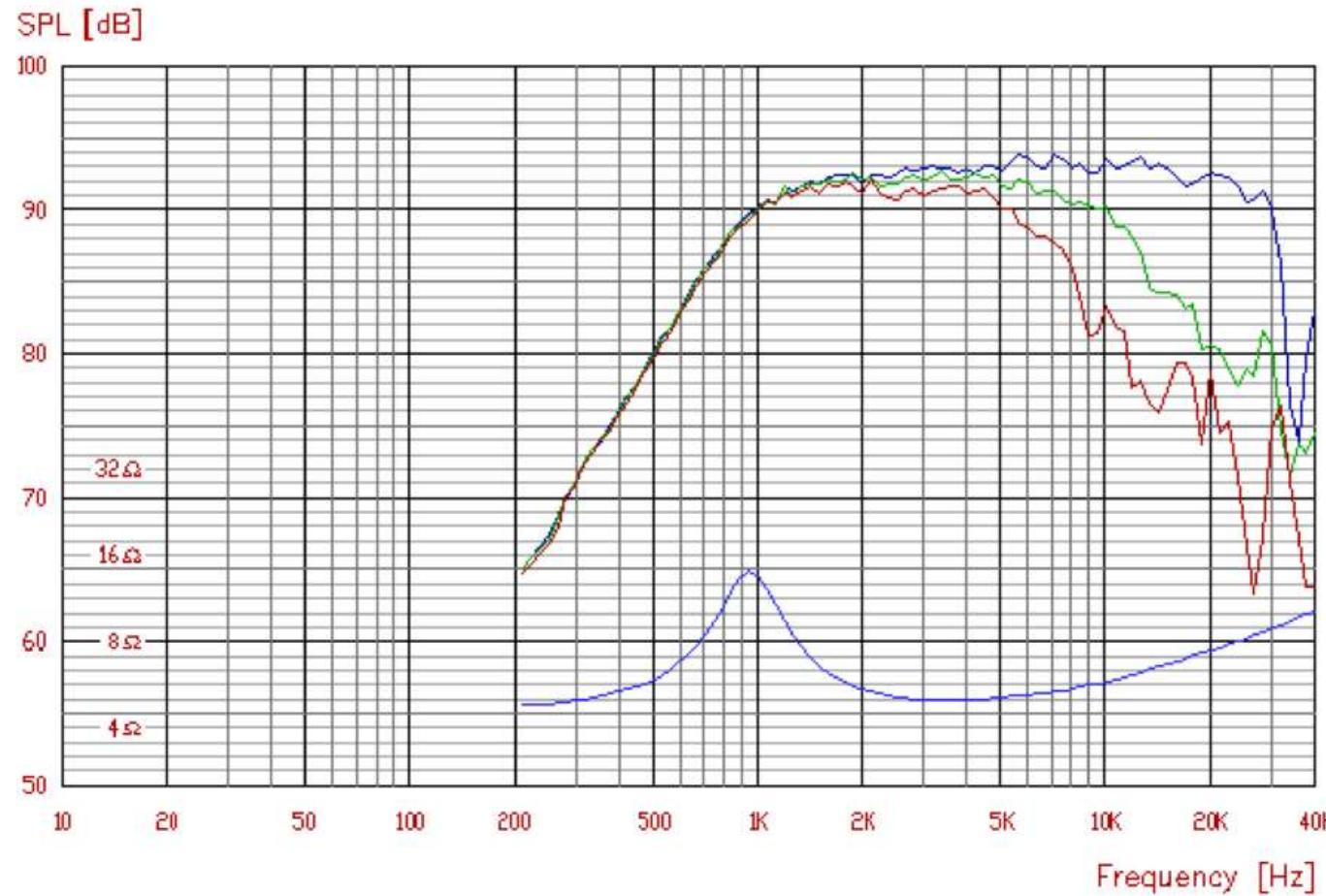
Frequency response of a loudspeaker

The acoustic frequency response or transfer function of a loudspeaker-driver shows the produced Sound Pressure Level (SPL) as a function of frequency at a distance of 1 m for a constant voltage of 2.83 V at the loudspeaker terminals (2.83 V at an 8Ω loudspeaker equals an input power of 1 Watt).



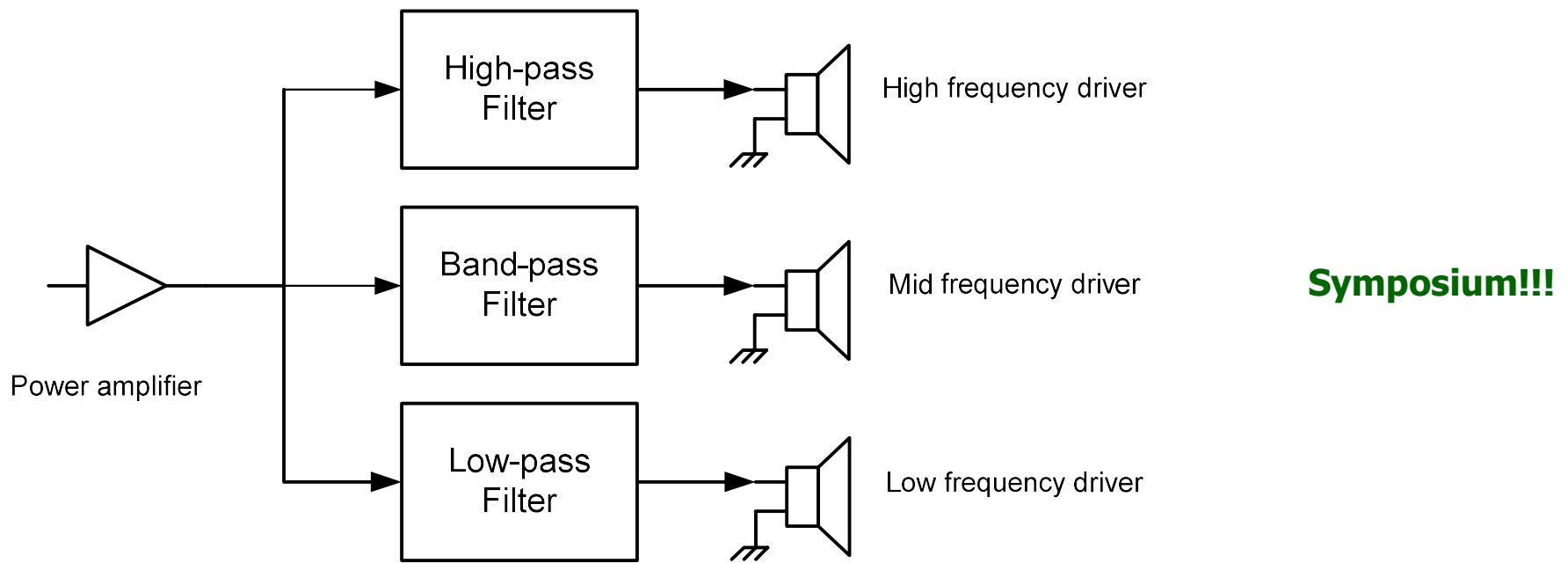
Impedance and sound pressure (at angles of 0, 30 and 60 degrees) as a function of frequency for a Peerless 830868 8 inch woofer.

Frequency response of a tweeter



Impedance and sound pressure (at angles of 0, 30 and 60 degrees)
as a function of frequency for a Vifa D27TG05-06 tweeter.

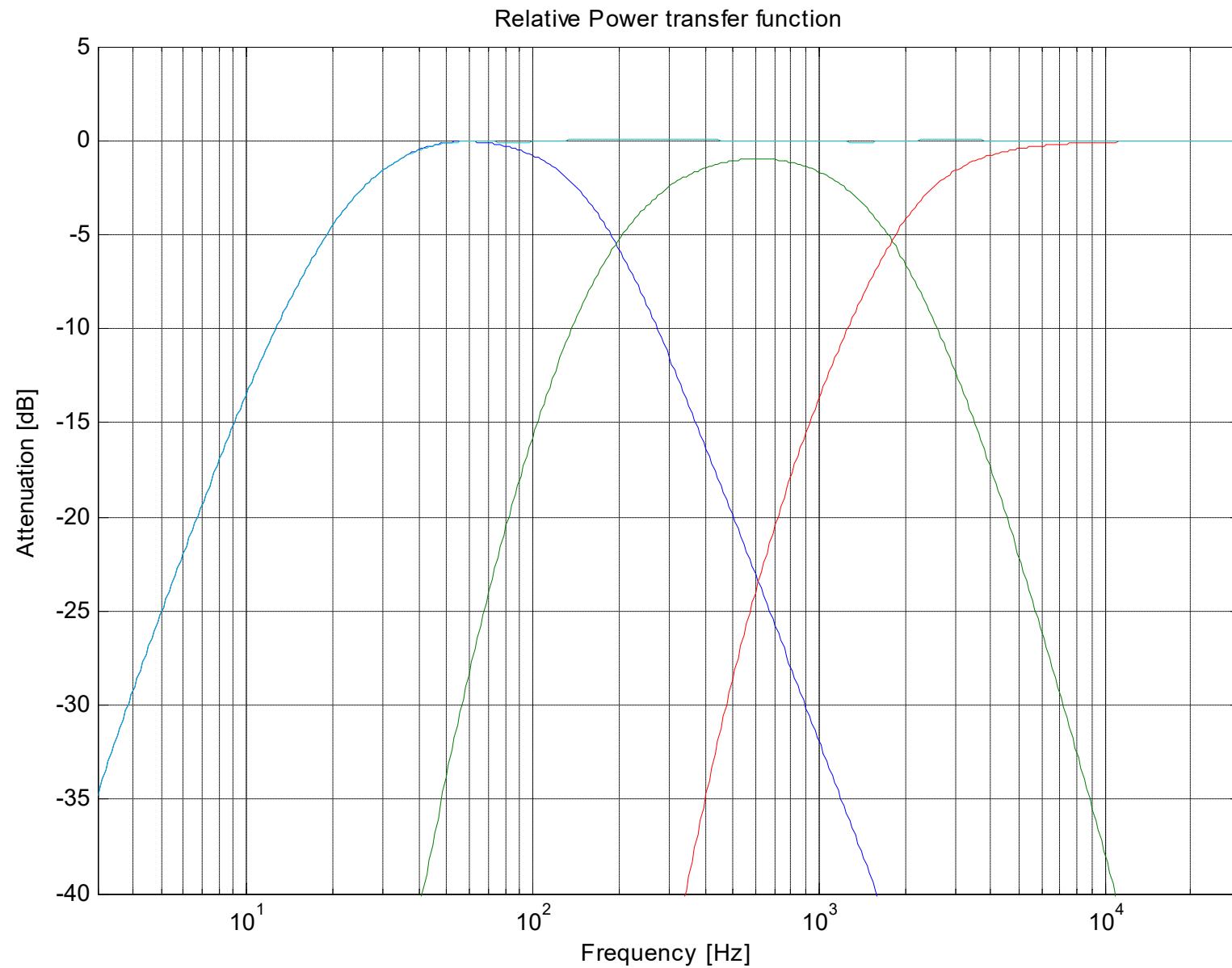
Loudspeaker system



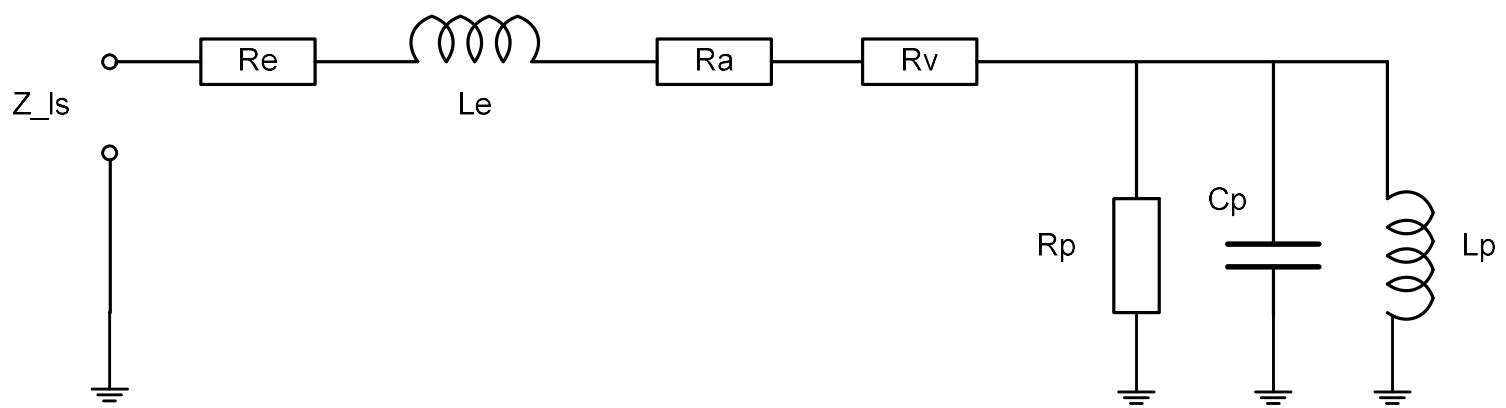
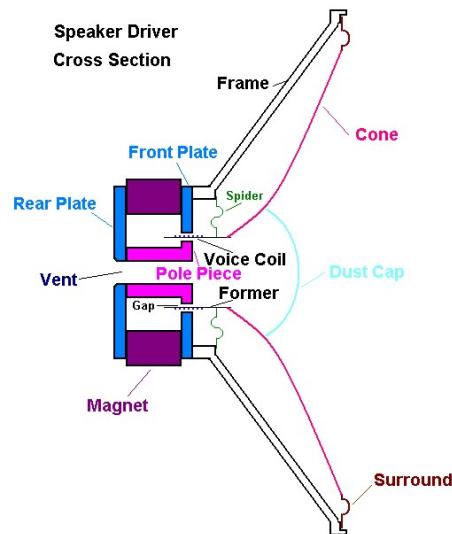
Loudspeaker: electro-mechanical transducer which converts an electric signal into an acoustic pressure wave

- ⇒ it is about the acoustic result: the bass, mid and treble should acoustically add up to a flat frequency response (transfer function) over the whole audio frequency range,
- ⇒ mutual influencing in the transition areas.

Combined frequency response



Electrical impedance of a loudspeaker (1)

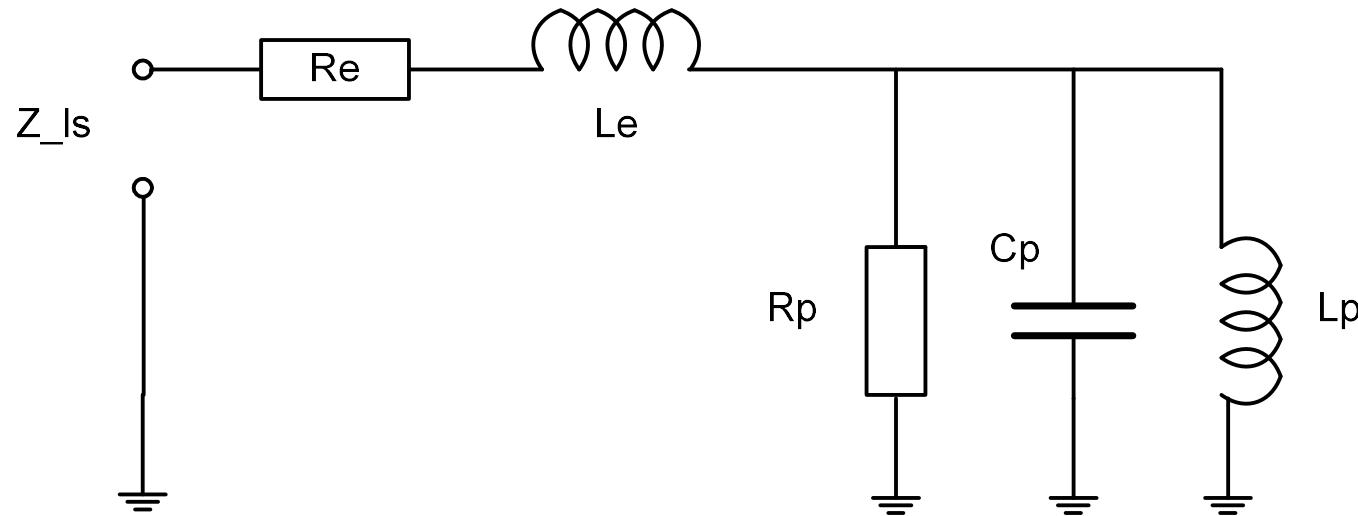


Impedance **model** of a loudspeaker-driver.

Here:

- R_e is the DC resistance of the voice coil
- L_e is the self-inductance of the voice coil
- R_a models the acoustic radiation resistance
- R_v models the mechanical loss resistance
- the parallel circuit of R_p , L_p and C_p , represents the electrical effects of the spring-load suspended cone (mass-spring system)

Electrical impedance of a loudspeaker (2)



Simplified impedance **model** of a loudspeaker-driver.

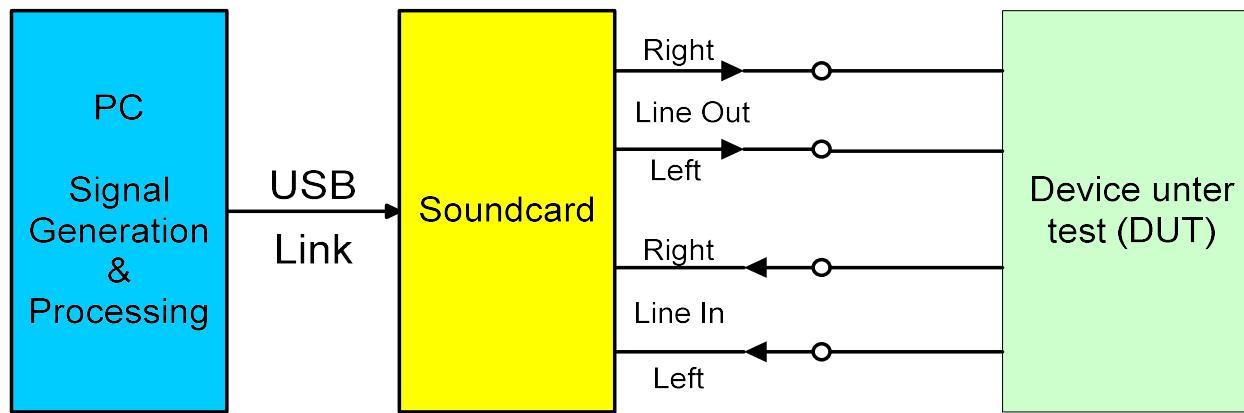
A practical loudspeaker has an **acoustic efficiency** in the order of 1%.

The mechanical power that is "lost" due to friction is also of the same order:

$$\Rightarrow R_a, R_v \ll R_e$$

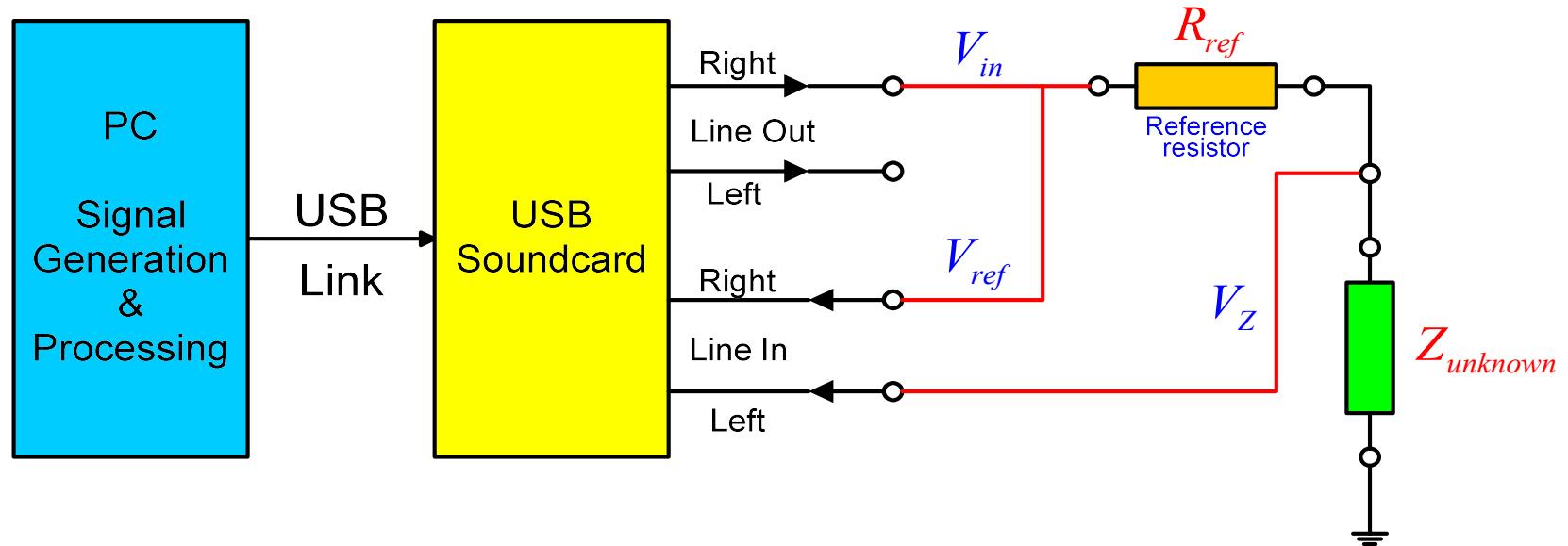
What happens with most of the electrical power we feed into a loudspeaker?

Basic measurement setup and measurement signals



- The **measurement signals** are generated in the PC and sent via the “Line Out” outputs of the soundcard to the “Device under test”.
- The output signals of the “DUT” are read via the “Line In” of the soundcard into the computer and **processed** to obtain the desired information.
- As measurement signal often a “white noise”-like is used, but in principle other measurement signals in the audio frequency band can be used as well.
White noise: all frequencies are present and contain the same amount of power.
- Some measurements will be performed with the help of a teaching assistance.

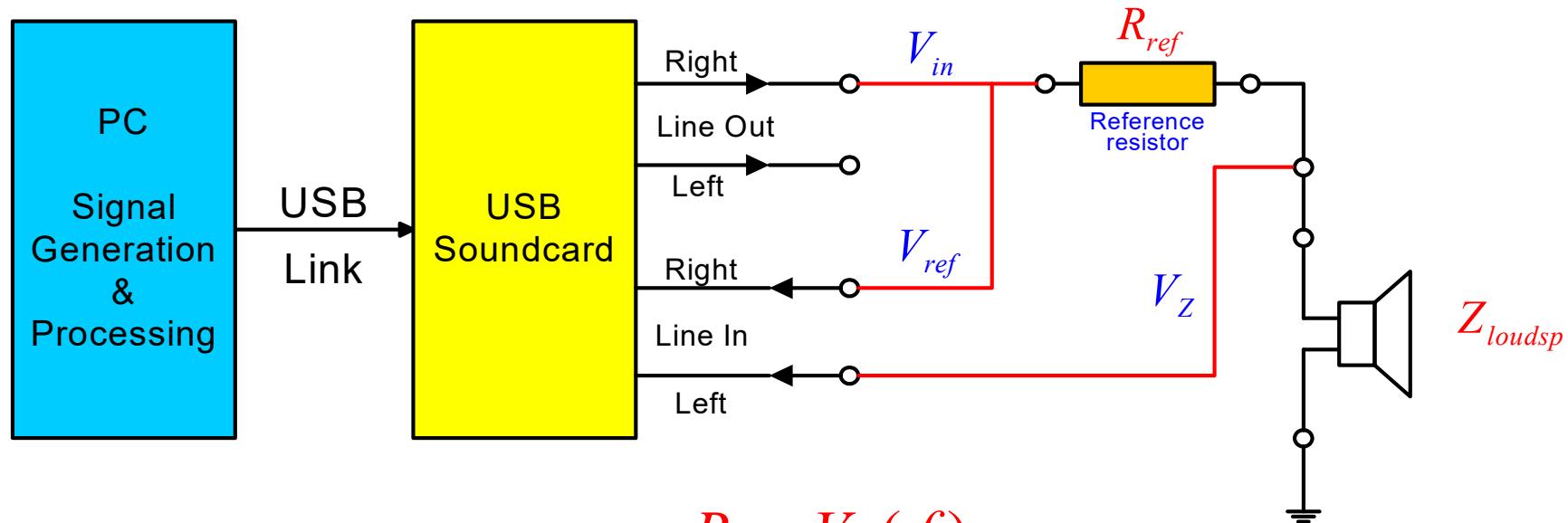
Measuring of an unknown impedance



$$Z_{unknown}(f) = \frac{R_{ref} \cdot V_Z(f)}{V_{ref}(f) - V_Z(f)}$$

- From the input voltage $V_{in}(f) = V_{ref}(f)$ and the measured voltage $V_Z(f)$ after voltage division across R_{ref} and $Z_{unknown}$, the absolute value and the phase of the unknown impedance is determined at all frequencies $f < 24$ kHz.

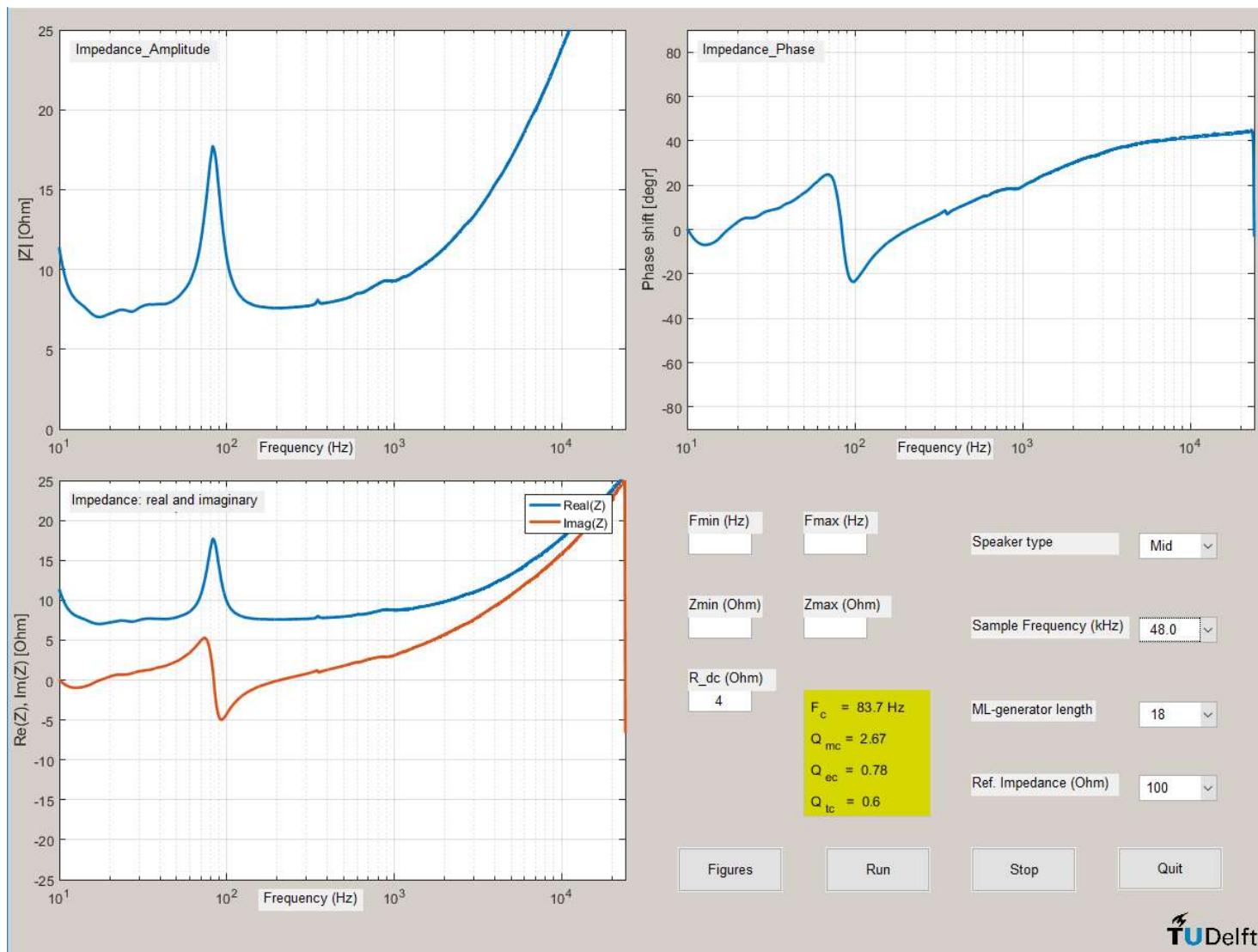
Measuring of loudspeaker parameters (1)



$$Z_{loudsp}(f) = \frac{R_{ref} \cdot V_Z(f)}{V_{ref}(f) - V_Z(f)}$$

- From the amplitude and phase of the loudspeaker impedance $Z_{loudsp}(f)$ a number of characteristic loudspeaker parameters can be derived: the resonance frequency f_c , the mechanical, electrical and total quality factors: Q_{mc} , Q_{ec} and Q_{tc} , and the Ohmic resistance R_e .
- This method can also be applied when the loudspeaker is mounted in a box (this will show slightly altered parameters compared to the unmounted loudspeaker).

Measuring of loudspeaker parameters (2)



R_dc: enter the resistance measured with an Ohm-meter.

Speaker type: select the type of loudspeaker to be measured: Bass, Mid, High.

ML-generator length: determines the duration of the measurement signal.

Ref. Impedance: choose the reference resistance equal to the one used in the measurement box (100 Ω).

Fmin, Fmax: herewith you set the minimum and maximum frequencies of the figure axes.

Zmin, Zmax: the same for the absolute value of the impedance.

Figures: Generates the figures. You will also obtain the data in Excel format to generate the figures for your logbook or report.

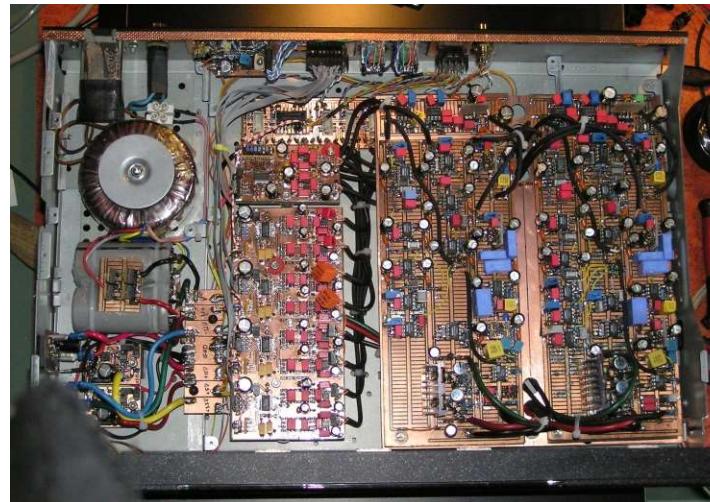
Run: start measurement.

Stop: user initiated stop of the measurement.

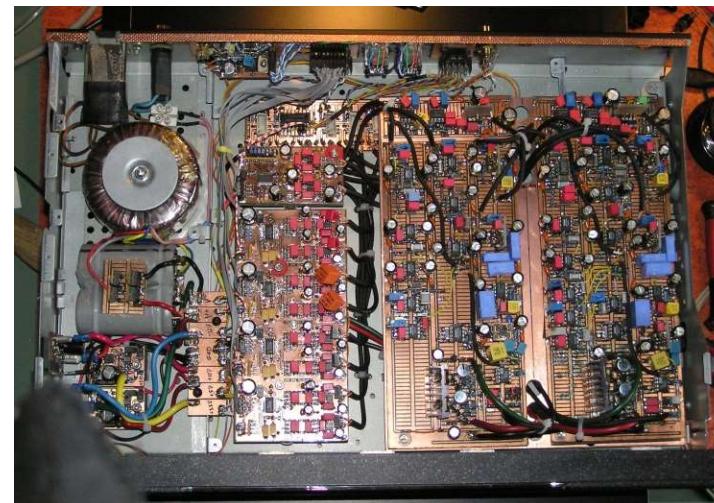
Where does this journey end ... ?



Or ... ?



Or ... ?



Or ... ?



Or ... ?



Or ... ?

